

# Assimilating Lagrangian data for parameter estimation in a multiple-inlet system



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## ABSTRACT

Numerical models of ocean circulation often depend on parameters that must be tuned to match either results from laboratory experiments or field observations. This study demonstrates that an initial, suboptimal estimate of a parameter in a model of a small bay can be improved by assimilating observations of trajectories of passive drifters. The parameter of interest is the Manning's  $n$  coefficient of friction in a small inlet of the bay, which had been tuned to match velocity observations from 2011. In 2013, the geometry of the inlet had changed, and the friction parameter was no longer optimal. Results from synthetic experiments demonstrate that assimilation of drifter trajectories improves the estimate of  $n$ , both when the drifters are located in the same region as the parameter of interest and when the drifters are located in a different region of the bay. Real drifter trajectories from field experiments in 2013 also are assimilated, and results are compared with velocity observations. When the real drifters are located away from the region of interest, the results depend on the time interval (with respect to the full available trajectories) over which assimilation is performed. When the drifters are in the same region as the parameter of interest, the value of  $n$  estimated with assimilation yields improved estimates of velocity throughout the bay.

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## 1. Introduction

Bottom stress is important to circulation in shallow water, and its inclusion in numerical models can have significant impacts on the simulation results. However, it is difficult to measure spatially-varying bottom stress directly in the field (Trowbridge et al., 1999; Sanford and Lien, 1999; Biron et al., 2004), and thus often stress is approximated with a bottom drag coefficient derived from laboratory experiments or by tuning numerical model simulations to observations, which usually involves iterations of model results that are time-consuming and costly (Cheng et al., 1999; Chen et al., 2015; Orescanin et al., 2016). Drag coefficients also can be estimated from observations of the flow by assuming a balance between pressure gradients and bottom stress (Feddersen et al., 2000; Seim et al., 2002; Apotsos et al., 2008; Kim et al., 2000; Orescanin et al., 2014). These coefficients have been estimated in other regions by assimilating sea-level data into numerical simu-

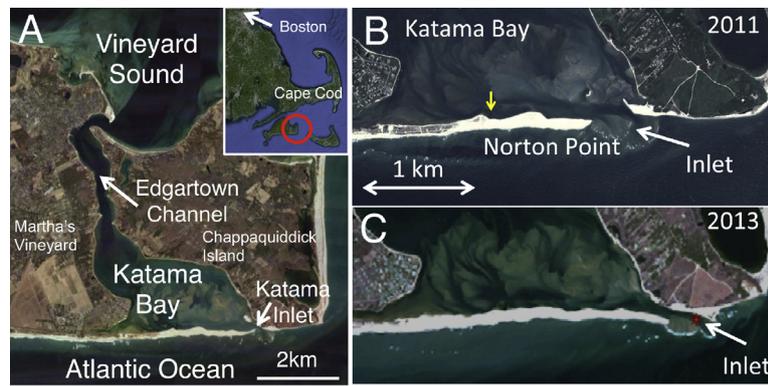
lations (Mayo et al., 2014). Here, the Manning's  $n$  drag coefficient in a multiple tidal inlet system on Martha's Vineyard, MA is estimated by assimilating observed Lagrangian drifter trajectories into a numerical model for sea level and circulation.

Martha's Vineyard is separated from Chappaquiddick Island by Katama Bay, which is connected to Vineyard Sound via Edgartown Channel and to the Atlantic Ocean via the ephemeral Katama Inlet (Fig. 1A). Norton Point, the sand spit between the bay and the Atlantic, was breached by a storm in 2007 (yellow arrow, Fig. 1B), forming Katama Inlet. Over the following years, the inlet became narrower, longer, and shallower as it migrated eastward (Fig. 1B, C), and friction became more important to sea level and circulation in the bay (Orescanin et al., 2016).

Data assimilation provides a framework for combining uncertain estimates from numerical models with noisy observations to estimate a variable that changes in time (Kalnay, 2003). For geophysical fluid flows, velocity fields and bathymetry can be estimated by assimilating Eulerian observations from in-situ sensors (Madsen and Cañizares, 1999; Oke et al., 2002; Kurapov et al., 2005; Wilson et al., 2010) or Lagrangian observations from drifting

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**Fig. 1.** A) Satellite image (Google Earth, 2012) of Katama Bay, Katama Inlet, and Edgartown Channel, with an inset showing the location of Katama Bay (red circle on Martha's Vineyard) relative to Boston and Cape Cod, B) Katama Inlet in 2011 showing the location of the initial breach of Norton Point (yellow arrow), and C) Katama Inlet in 2013 during drifter deployments. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

sensors (Ide et al., 2002; Mariano et al., 2002; Molcard et al., 2005, 2006; Salman et al., 2006; Apte et al., 2008). Drifters follow (approximately) the motion of fluid parcels, and assimilation of their trajectories leads to improved estimates of large-scale circulation patterns (Taillandier et al., 2006; Jacobs et al., 2014) and flows in vortices (Vernieres et al., 2011). Lagrangian observations also have been assimilated in models that estimate the topography in a laboratory channel (Honnorat et al., 2010) and the bathymetry in a river (Landon et al., 2014). Synthetic experiments have compared the Eulerian flow fields estimated by assimilating velocities derived from Lagrangian data (so-called pseudo-Lagrangian data assimilation) and by assimilating Lagrangian trajectories directly, and the results show that the direct assimilation of trajectories outperforms pseudo-Lagrangian data assimilation (Molcard et al., 2003).

In 2011, when Katama Inlet was open (Fig. 1B), current meters were deployed throughout the bay (Orescanin et al., 2014; 2016). A numerical model (ADCIRC, Luettich and Westerink, 1991) of the circulation in the bay at this time was developed, using boundary conditions from pressure gauges deployed in 2011, and the Manning's  $n$  coefficient in the region of Katama Inlet was tuned to match the data from the current meters in 2011. In 2013, after the inlet had begun to migrate and narrow (Fig. 1C), current meters were again deployed throughout the bay. Results from the numerical model using boundary conditions from the gauges deployed in 2013, but with the same estimates of Manning's  $n$  from 2011, were compared with the 2013 observations from the current meters. Orescanin et al. (2016) found that discrepancies between the 2013 observations and the numerical model were due to changes in friction, and therefore, the value of Manning's  $n$  in Katama Inlet estimated from 2011 data was suboptimal when modeling the 2013 system.

Here, drifter tracks observed in the Katama Bay system are assimilated into a numerical circulation model (ADCIRC) to estimate the bottom friction. The model uses bathymetry measured throughout the system and is driven with observed tides, and simulations with and without assimilating drifter data are compared with Eulerian observations of currents in Katama Bay. As a proof of concept, synthetic observation experiments are performed first. Experiments assimilating real drifter data are performed next. Results from assimilating synthetic and real drifter trajectories in two distinct regions of Katama Bay are compared.

## 2. Numerical model and observations

### 2.1. Numerical model of Katama Bay

Sea level and depth-averaged currents in Katama Bay are simulated with the two-dimensional version of the Advanced Circula-

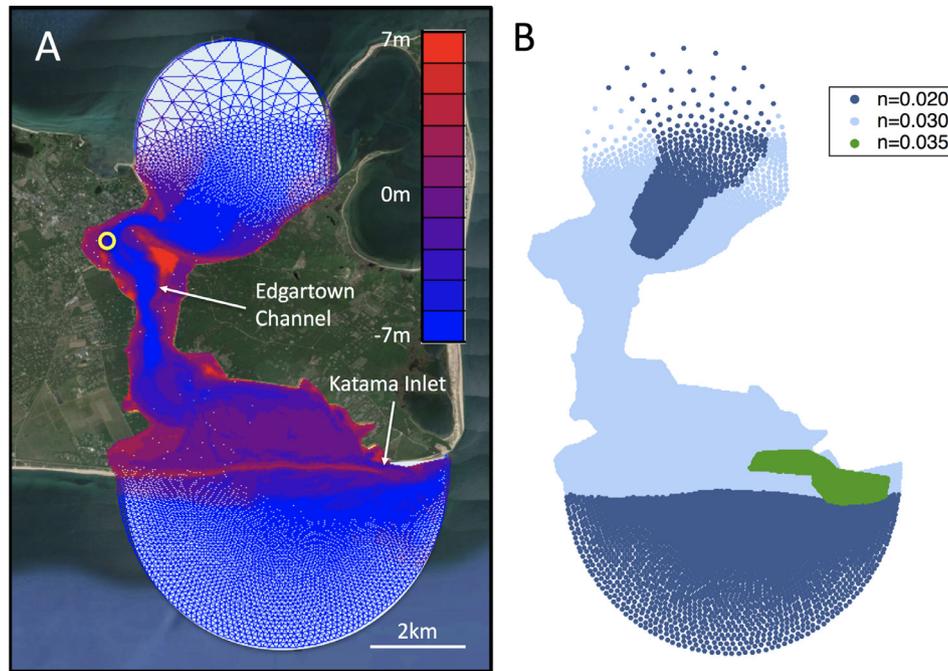
tion Model (ADCIRC, Luettich and Westerink, 1991), which solves a version of the shallow water equations via a finite-element method. This model assumes no stratification in the domain; this was supported by observations in Katama Bay. Casts from CTD (conductivity, temperature, depth) instruments throughout the system show little to no temperature or salinity stratification. Within the bay, the depths are very shallow, so this is expected. Offshore in Vineyard Sound and the Atlantic, in depths less than 10 m, the same lack of vertical structure was observed. Winds were light ( $< 2$  m/s) and waves were small ( $< 1$  m) during the drifter deployment periods, and are not included here. The numerical grid consists of a finite-element triangular mesh with spacing ranging from 10 m in the inlets and 15 m in the bay to 200 m outside the inlets in both the Atlantic Ocean and Vineyard Sound (Fig. 2A). Bathymetry (5 to 20 m horizontal and 0.05 m vertical resolution) in the bay, the inlets, and the ebb tidal delta (Fig. 2A) was measured in 2013 with GPS and an acoustic altimeter mounted on a personal water craft, and interpolated onto the model grid (Orescanin et al., 2016). Pressure gauges and current meters were co-located at ten locations within Edgartown Channel, Katama Bay, and Katama Inlet (orange circles in Fig. 3) (Orescanin et al., 2016). The northern boundary of the model is forced with the sea-level observations in Edgartown Harbor (yellow circle in Fig. 2A), and the southern boundary is forced with observations from the Martha's Vineyard Coastal Observatory (12 m depth, 4 km west of Katama Inlet; not shown).

To estimate quadratic bottom stress, the model converts bottom roughness given by a user-defined value of Manning's  $n$  (units  $s/m^{1/3}$ ) at each node to an equivalent quadratic drag coefficient given by:

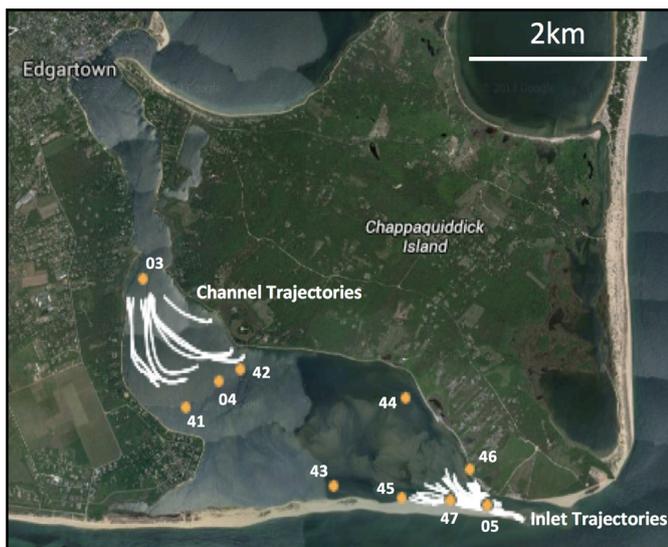
$$C_d(t) = \frac{gn^2}{(D + \eta(t))^{1/3}}, \quad (1)$$

where  $g$  is gravity,  $t$  is time,  $D$  is the local mean depth, and  $\eta(t)$  is the water surface elevation above  $D$  (Luettich and Westerink, 1991).

The Katama Bay domain is divided into several subregions based on bathymetry, each with a different value of Manning's  $n$  (see Fig. 2B.) In the original 2011 simulations, the deep boundary regions (dark blue in Fig. 2B) outside of the bay were assigned the value  $n = 0.020 s/m^{1/3}$ , which is standard for open water. The bay (light blue) was assigned  $n = 0.030 s/m^{1/3}$ , which was calculated by converting the bottom stress estimated from a pressure gradient balance (Orescanin et al., 2014) into  $n$  using an average depth of the bay. However, model-data comparisons (Orescanin et al., 2016) suggested that the friction coefficient needed to be increased to  $n = 0.035 s/m^{1/3}$  in an area surrounding Katama Inlet (green area in Fig. 2B) in 2011. This spatial and temporal variation in  $n$  is



**Fig. 2.** A) Google Earth image of the Katama system with seafloor and land elevation contours (colors, scale on right), the grid mesh, and the Edgartown Harbor pressure gauge (yellow circle) and B) the bathymetrically-defined subregions with different friction factors ( $n$ ; values for the colors are given in the legend, units  $\text{s/m}^{1/3}$ ). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 3.** Trajectories of real drifters deployed August 20, 2013 for approximately 140 min (Channel Trajectories) and August 22, 2013 for approximately 110 min (Inlet Trajectories) in Katama Bay. Orange circles are locations of acoustic Doppler current meters (water depths  $< 2$  m) and profilers (depths  $> 2$  m). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

due mainly to changes in bedforms; for example, sand waves and dunes were observed throughout the system, and tended to migrate over time. These values of Manning's  $n$  are typical in tidal inlets, including multiple tidal inlet systems (Mehta and Joshi, 1998; Kraus and Militello, 1999; Friedrichs and Madsen, 1992; Friedrichs, 1995; Dias et al., 2009).

By iteratively simulating the 2011 circulation, Manning's  $n$  was estimated as the value that minimized the difference between observed and simulated kinetic energy in the bay circulation (Orescanin et al., 2016). The tuning required several different model simulations, as well as a method for determining

which value is optimal, because varying  $n$  can improve kinetic energy estimates in the inlet while degrading estimates elsewhere in the bay. For the estimation of the 2011 circulation, the root mean squared errors between the simulated and observed velocity kinetic energies, tidal currents, and sea-level amplitudes and phases were minimized. In particular,  $n$  was tuned until the errors at each of the seven observation locations were less than 15%, while minimizing the total error throughout the domain (Orescanin et al., 2016, especially Table 1). The Katama Inlet bathymetry changed substantially between 2011 and 2013 (compare Fig. 1C with 1B), and simulations using the 2013 bathymetry and the 2011-estimated  $n$  had decreased skill within Katama Inlet (Orescanin et al., 2016). Note also that the flow has the greatest velocities in the inlet, and therefore changes in  $n$  here have large effects throughout the system (Orescanin et al., 2016). Here, Lagrangian drifter data from 2013 field experiments are assimilated into the model to improve the estimates of friction in Katama Inlet in 2013.

## 2.2. Drifter observations in 2013

In August 2013, several drifter deployments were conducted with twelve drifters released in multiple deployments over several days. On August 20, the drifters targeted Edgartown Channel, and on August 22, they targeted Katama Inlet (Fig. 3). The surface tracking drifters used herein are a modified version of drifters deployed in the surf zone (MacMahan et al., 2009; Fiorentino et al., 2012) and rivers (Landon et al., 2014), both in body shape and type of handheld GPS. These drifters were deployed together in the inner shelf and visually behaved similarly. The GPS used on the 2013 Katama drifters is a Locosys GT-31, which provides accurate relative position useful for velocity measurements. The Locosys GPS has successfully measured surfzone velocities and trajectories (McCarroll et al., 2014) and surface gravity wave elevations (Herbers et al., 2012). The inlet drifters were also deployed as part of an experiment in the inner shelf of the Gulf of Mexico. The drifter trajectories compared well to acoustic Doppler current

profiler (ADCP) surface velocity estimated trajectories (Roth et al., 2017).

### 3. Overview of Lagrangian data assimilation

Lagrangian data can be assimilated directly or indirectly. In pseudo-Lagrangian data assimilation (Molcard et al., 2003), sequential positions of the drifters are converted to Lagrangian velocities, which are then assimilated into the model. Fully Lagrangian data assimilation uses the positions of the drifters directly, such as in the augmented vector approach (Kuznetsov et al., 2003), in which the positions of the drifters are appended to the state vector at each time step. With this approach, to assimilate observations of a single drifter following the flow into a two-dimensional velocity field, the augmented vector at time  $t$  is  $[u, v, x, y](t)$ , where  $u$  and  $v$  are a representation of the velocity field at each model grid point at time  $t$ , and  $(x, y)$  is the position of the drifter at that time.

Here, the focus is on estimating  $n$  as a parameterization of the flow field, so the state vector is  $[n, x_1, y_1, \dots, x_{N_D}, y_{N_D}]$  for  $N_D$  drifters. The velocity  $[u, v]$  is not estimated directly from the assimilation, and thus does not appear in the state vector, although the evolution of the drifter positions depends on the time-variable velocity field, which depends on  $n$ .

#### 3.1. Ensemble Kalman filter

The data assimilation method used here is the ensemble Kalman filter (EnKF) (Evensen, 1994), which is used both operationally (Wei et al., 2006) and in test problems, including Lagrangian data assimilation (Salman et al., 2006, 2008). The EnKF assimilates consecutive observations serially. At each time step, the best estimate and a quantification of its uncertainty are provided by an ensemble of possible realizations. When an observation is available, the ensemble is updated to reflect the new information. Here, the EnKF is reviewed briefly in the context of Lagrangian data assimilation for parameter estimation.

Let the state vector be given by  $\mathbf{z}(t) = [n, x_1(t), y_1(t), \dots, x_{N_D}(t), y_{N_D}(t)]$ . At times  $t_1, t_2, \dots, t_f$  drifters are observed at positions  $\mathbf{q}_{obs}$ , so that

$$\mathbf{q}_{obs}(t_k) = \mathbf{H}\mathbf{z}(t_k) + \epsilon_k \quad (2)$$

where  $\mathbf{H} = [0 \ \mathbf{I}]$  is the observation operator in the augmented vector setup, and  $\epsilon_k \sim \mathcal{N}(0, \mathbf{R})$  where  $\mathbf{R}$  is the observational error covariance. The observation errors are assumed to be uncorrelated in time, independent, and Gaussian so that  $\mathbf{R} = \sigma_R^2 \mathbf{I}$  is diagonal.

Assume that at time  $t_{k-1}$ , there is an ensemble  $\{\mathbf{z}_i(t_{k-1})\}$  for  $i = 1 \dots N_e$ , and the next available observation is at time  $t_k$ . The forecast ensemble is computed by evolving each ensemble member forward under the dynamics. Although the parameter being estimated could evolve under a dynamic model as well, here the parameter remains the same between observation times, but the flow determined by that parameter evolves according to the numerical model (in this case, ADCIRC.) Each ensemble member's drifters simultaneously are advected passively under that velocity field, giving the forecast ensemble at time  $t_k$ ,  $\{\mathbf{z}_i^f(t_k)\}$ , which will be updated to reflect the observation. The EnKF update step, also known as the *analysis* step, is applied to each ensemble member according to:

$$\mathbf{z}_i^a = \mathbf{z}_i^f + \mathbf{P}^f \mathbf{H}^T (\mathbf{H} \mathbf{P}^f \mathbf{H}^T + \mathbf{R})^{-1} (\mathbf{H} \mathbf{z}_i^f - [\mathbf{q}_{obs} + \eta_i]) \quad (3)$$

$$\mathbf{P}^f = \frac{1}{N_e - 1} \sum_{i=1}^{N_e} (\mathbf{z}_i^f - \bar{\mathbf{z}}^f) (\mathbf{z}_i^f - \bar{\mathbf{z}}^f)^T$$

where  $\mathbf{P}^f$  is the sample covariance of the forecast ensemble and  $\eta_i \sim \mathcal{N}(0, \mathbf{R})$  for the perturbed observation formulation of the EnKF (Evensen, 2003). This step takes place entirely at time  $t_k$ , and

thus the time dependence has been dropped. The forecast-analysis cycle is then repeated for each available consecutive observation time.

Here, the scalar Manning's  $n$  in the Katama Inlet area (green region in Fig. 2) is estimated using drifter trajectories located throughout the bay. Thus, only  $n$  and the drifter positions are updated at each analysis step; in the forecast step, the full velocity and elevation fields of the entire domain evolve according to ADCIRC with the latest updated value of  $n$  in Katama Inlet.

#### 3.2. Observing system simulation experiments

The method is tested in an artificial scenario known as an observing system simulation experiment (OSSE), in which the same model used in the forecast step of the assimilation method also is used to create a synthetic truth consisting of time series of both the velocity field and the drifter positions. Random (Gaussian) perturbations are then added to the true drifter trajectories to simulate noisy observations. An initial ensemble of the flow and drifters is generated by perturbing the true initial value of Manning's  $n$  in Katama Inlet and the true drifter positions. This yields an ensemble of different flow states, each consistent with a perturbed value of  $n$ , and each with different initial drifter positions. The performance of the data assimilation method is then judged based on its ability to recover the true value of  $n$  in the inlet from the perturbed initial ensemble and the noisy observations.

Two OSSEs are run. One assimilates drifter trajectories from Katama Inlet (thick white curves in Fig. 4), and the other assimilates trajectories from Edgartown Channel, located north of the inlet subdomain (thin white curves in Fig. 4). The drifter release times and locations are designed to mimic the real data available from August 2013. In both experiments, the synthetic truth is a 6 h time series of the velocity field generated with Manning's  $n = 0.035 \text{ s/m}^{1/3}$  in the inlet and the trajectories from 13 drifters. The initial ensemble of drag coefficients  $\{n_i\}$  for  $i = 1 \dots N_e = 30$  is drawn from a normal distribution with mean  $0.025 \text{ s/m}^{1/3}$  and standard deviation  $0.005 \text{ s/m}^{1/3}$ . This is a common ensemble size for this size problem (Houtekamer and Mitchell, 2001; Mitchell et al., 2002; Evensen, 2003). Decreasing the ensemble size to  $N_e = 10$  degrades the performance, but  $N_e = 20$  yields similar results as  $N_e = 30$ . In practice, some *a priori* knowledge of the feasible range



Fig. 4. Synthetic drifter trajectories in Katama Bay. Thin white trajectories are from the drifters released on model date August 20 in Edgartown Channel, and thick white trajectories are from drifters released on model date August 22 just outside Katama Inlet.

of values is necessary in order to choose the initial ensemble mean and spread. For the synthetic experiments here, the initial ensemble is defined relatively far from the truth (the mean is two standard deviations less than the true value of  $n$ ) to determine whether the assimilation can recover the truth even under these conditions.

The observation error of the drifters has mean 0 and standard deviation  $\sigma_R = 25\text{m}$ . This is larger than the value of approximately 2 m given by MacMahan et al. (2009) as the error of the real drifter positions, to prevent the assimilation ensemble from collapsing onto the observations too quickly and resulting in filter divergence. Here, “filter divergence” refers to the collapse of the ensemble onto the incorrect estimate of  $n$ , but it could also result in an estimate of the uncertainty surrounding  $n$  that is not large enough (due to an ensemble spread that is too small). Filter divergence is often a result of applying an approximately linear method (that is, the EnKF) to a nonlinear problem (such as drifter trajectories in a nonlinear flow) and has been demonstrated in the Lagrangian data assimilation setup (Apte et al., 2008; Slivinski et al., 2015). In a system that has only weakly nonlinear characteristics, the EnKF can avoid divergence if larger errors are included (Mitchell et al., 2002). Although overestimating observation error can potentially have detrimental effects, such as increasing the time it takes for the ensemble estimate to converge and providing an artificial lower bound on the errors in the estimates, the results in the following section suggest that the assimilation worked well with the chosen values: the ensemble does not collapse too early nor does it diverge. The time between subsequent observations  $\Delta t$  is tested for  $\Delta t = 1, 5,$  and  $10$  min. The veloc-

ity fields for both the synthetic truth and the initial ensemble are spun up with their respective values of  $n$  for several days, so that all the simulations have reached equilibrium before assimilation begins.

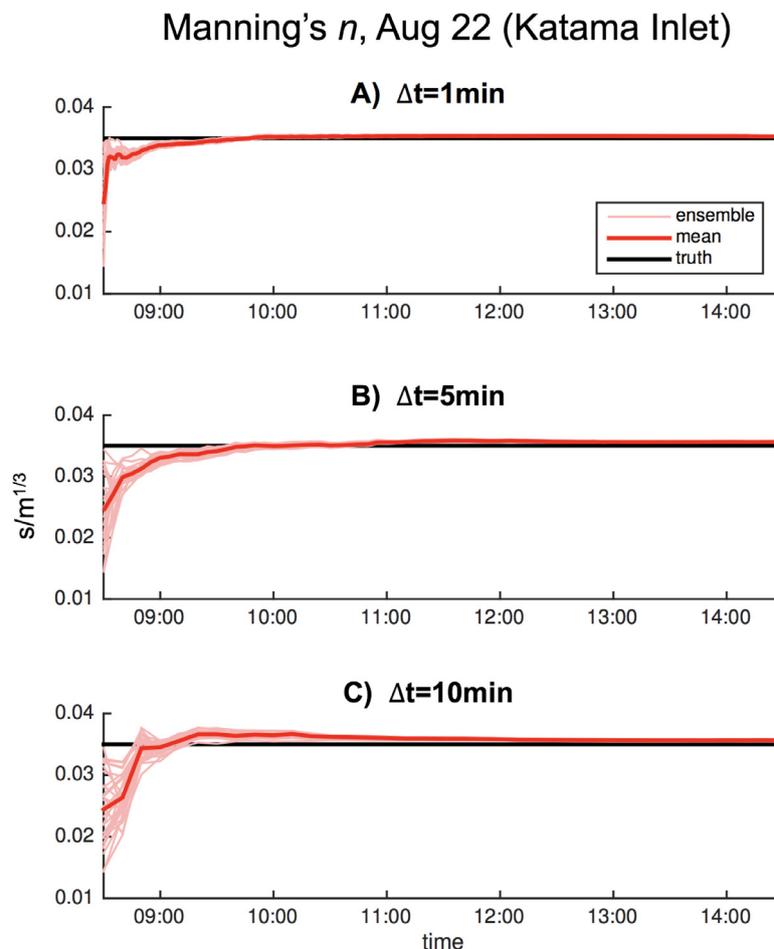
#### 4. Results from synthetic experiments

##### 4.1. Drifters within the subdomain of interest

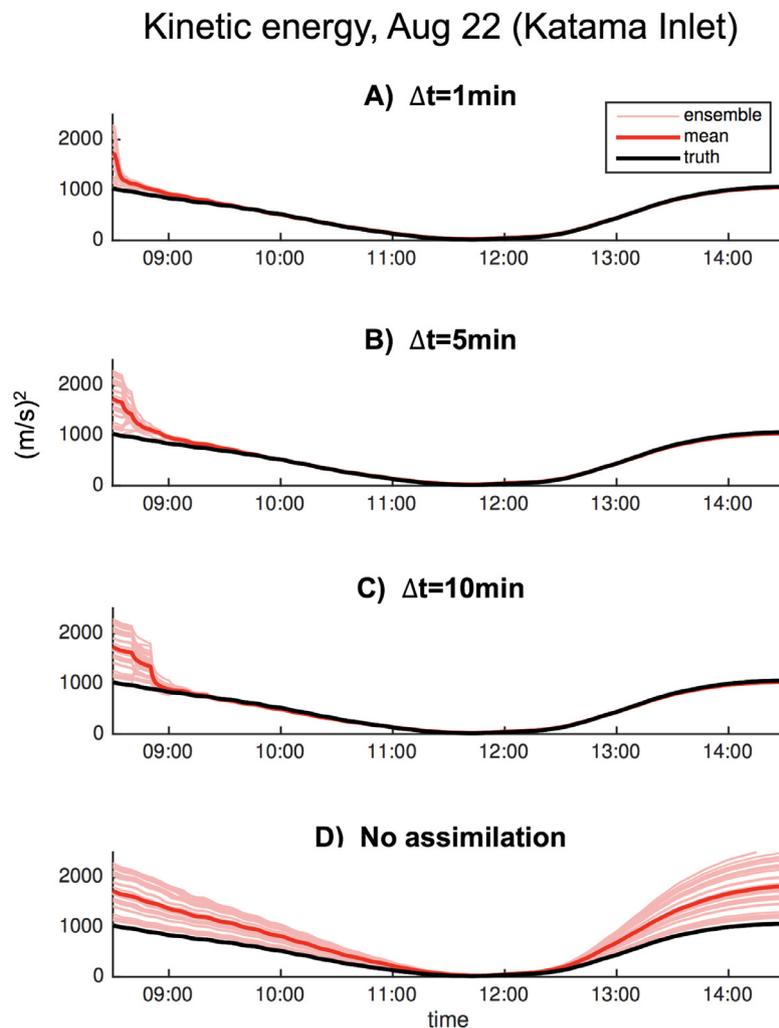
OSSEs are run with drifters released just outside Katama Inlet when the flow is from south to north into the inlet, through the bay, and out through Edgartown Channel to Vineyard Sound. The drifter deployment times and locations are chosen to mimic the real observations, so  $N_D = 13$  synthetic drifters are released (in the numerical model) just outside the inlet starting at 8:30 am (EDT) August 22, 2013. To study the convergence of the estimates of  $n$ , the data are assimilated over a period of 6 h, significantly longer than the 1–2 h-long time windows of the real drifter observations.

For each of the  $\Delta t$ , the assimilation estimates  $n$  fairly well, converging after about 60 min (Fig. 5). However, for  $\Delta t = 10$  min, the assimilation initially overestimates  $n$  slightly, and gradually decreases to the truth over the six hour window (Fig. 5C).

The estimates of kinetic energy, defined as 0.5 times the sum of squared velocity over all grid points  $i$ :  $\frac{1}{2} \sum_i (u_i^2 + v_i^2)$  for the three data assimilation experiments, also converge within 60 min to the synthetic true values (Fig. 6 (A–C)). A “free run”, in which the initial ensemble members are each integrated forward without assimilation for 6 h with the initial value of  $n$  remaining constant, has



**Fig. 5.** Ensemble (thin light red curves) and mean (thick red curves) estimates for Manning's  $n$  versus assimilation time on August 22, when drifters were released in Katama Inlet, for  $\Delta t =$  (A) 1, (B) 5, and (C) 10 min. The black line is  $n = 0.035 \text{ s/m}^{1/3}$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 6.** Ensemble (thin light red curves) and mean (thick red curves) estimates of kinetic energy versus assimilation time on August 22, when drifters were released in Katama Inlet, for  $\Delta t=$  (A) 1, (B) 5, and (C) 10 min, as well as the case with no data assimilation (D). The black curves are the synthetic “truth” from the simulation with  $n = 0.035 \text{ s/m}^{1/3}$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

poorer performance than the assimilation runs (compare Fig. 6D with A–C). These results demonstrate that changing the friction (via assimilation) on these time scales has near-immediate effects on the total kinetic energy in the model, and thus, the assimilated ensemble predicts the correct kinetic energy as quickly as it estimates the correct value of the drag coefficient.

#### 4.2. Drifters in Edgartown Channel

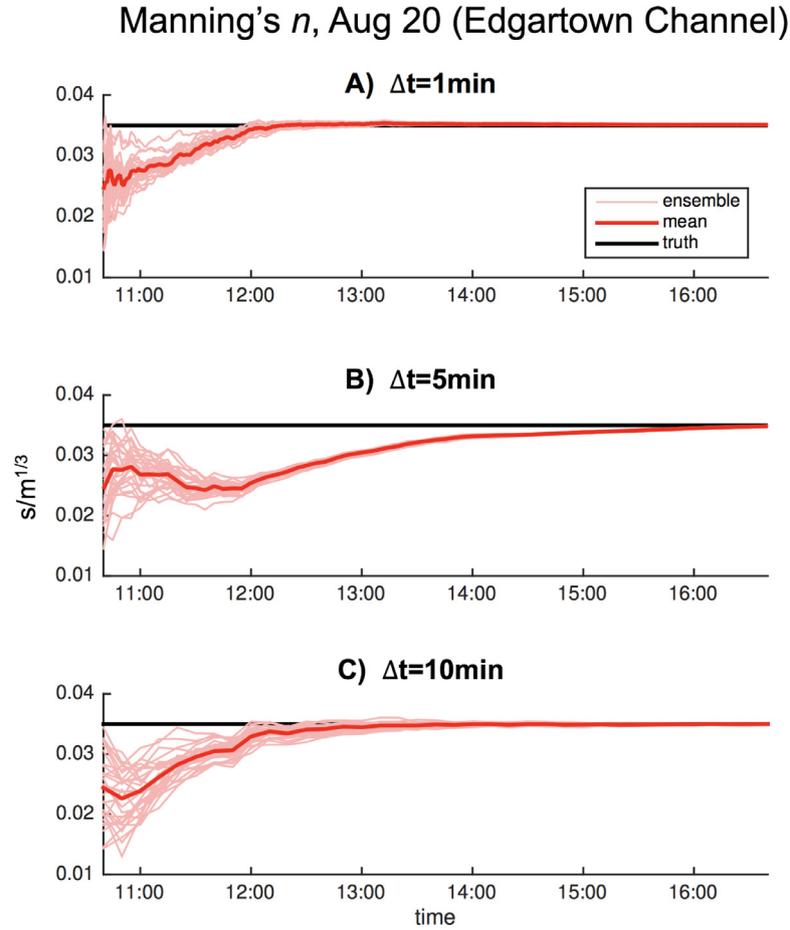
Three additional experiments are run with the same setup as above, but with the drifters released in Edgartown Channel. Again, the deployment time (10:40 am August 20, 2013) and initial locations of the 13 drifters are chosen to match the real data, and observations are assimilated for six hours for  $\Delta t = 1, 5,$  and  $10$  min. Although the drifters never approach the inlet subdomain in which the drag coefficient is estimated, the assimilation converges to the correct “true” value of  $n$  (Fig. 7). However, assimilating drifters in Edgartown Channel results in a longer time to convergence than assimilating drifters in the inlet. For  $\Delta t = 1$  min, the ensemble takes about 90 min to converge onto the truth (Fig. 7A), and for  $\Delta t = 10$  min, it takes about 2 h (Fig. 7C). For  $\Delta t = 5$  min, the ensemble initially diverges from the truth, and takes approximately 6 h to converge (Fig. 7B). This is likely due to a combination of nonlinearity and random noise that has a stronger effect on the assimilation when the observations are farther away from the

region of interest, and is discussed below in more detail. Similar to the releases in Katama Inlet (Fig. 6), assimilation estimates of the kinetic energy converge to the true values at the same rate as  $n$  converges (Fig. 8).

#### 4.3. Discussion

As expected, the assimilation of drifters in the same spatial location (Katama Inlet) as the estimated  $n$  leads to quicker convergence to the true  $n$  than the assimilation of drifters in Edgartown Channel. This is consistent with the results of Salman et al. (2008), who showed that local structures within a flow field are well-approximated when the drifters stay close to those structures (eg, when the drifters are trapped in a vortex), whereas global flow properties are estimated best when the drifters cover most of the domain (eg, when the drifters are spread out and some follow a jet stream in the flow). Therefore, the performance of the Lagrangian data assimilation algorithm will depend on the spatial location of the drifters and their trajectories.

Although the performance degrades slightly when the time between observations of drifters in Katama Inlet is increased, the assimilation estimates the correct value of  $n$  within about an hour for each  $\Delta t$ . Conversely, when drifters in Edgartown Channel are assimilated, the performance of the assimilation depends more



**Fig. 7.** Ensemble (thin light red curves) and mean (thick red curves) estimates of Manning's  $n$  versus assimilation time on August 20, when drifters were released in Edgartown Channel, for  $\Delta t =$  (A) 1, (B) 5, and (C) 10 min. The black line is  $n = 0.035 s/m^{1/3}$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

strongly on the time between observations, and does not improve monotonically as the time between observations decreases.

To determine why assimilating trajectories from Katama Inlet results in significantly faster convergence than assimilating Edgartown Channel trajectories, especially for intermediate  $\Delta t = 5$  min, consider the time it takes the kinetic energy in the bay to adjust and equalize after an abrupt change in the drag coefficient in the inlet. A crude approximation of the adjustment time is the time required for a long gravity wave to propagate over the largest dimension of the bay  $l_{max}$  in water depth  $d$ , and for a reflected wave to return to the source over the same path:

$$\begin{aligned}
 T_{\text{adjustment}} &\approx 2 \left( \frac{l_{max}}{\sqrt{gd}} \right) \\
 &\approx 2 \left( \frac{2 \times 10^3 m}{(9.8 * 4)^{1/2} m/s} \right) \\
 &\approx 600 s.
 \end{aligned} \tag{4}$$

Thus, the intrinsic time for Katama Bay to adjust to changes in  $n$  in the inlet is approximately 10 min.

To determine how long it takes the velocity field and the drifters to adjust to the new value of Manning's  $n$ , the system was run for 4 days with  $n = 0.035 s/m^{1/3}$  in the inlet and constant north-to-south tidal forcing, similar to the case when the drifters are released in Edgartown Channel. At the beginning of the fifth day, simulations with  $n = 0.01, 0.02, 0.03, 0.035, 0.04, 0.05,$  and  $0.06 s/m^{1/3}$  were run. In each experiment, drifters are released

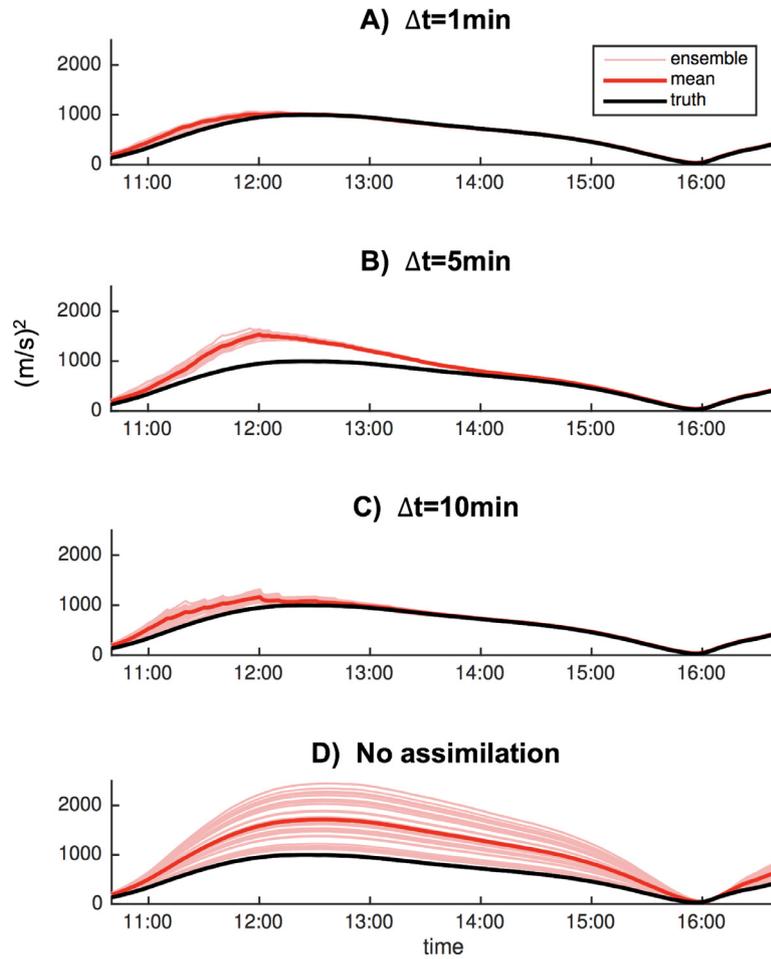
in Edgartown Channel at the same locations as the synthetic experiment above. Each situation is simulated for 1 hr, with no assimilation.

For a range of initial values of  $n$ , the kinetic energy averaged over the entire domain converges about 25 min after  $n$  is changed, although for the simulations with the largest and smallest values of  $n$ , the kinetic energy oscillates slowly (Fig. 9). A change of  $0.005 s/m^{1/3}$  in  $n$  from the true values results in convergence after about 10 min. Changing  $n$  by  $0.025 s/m^{1/3}$  results in about a 50% change in kinetic energy (e.g., compare the blue ( $n = 0.010$ ) with the purple ( $n = 0.035$ ) curve and compare the purple ( $n = 0.035$ ) with the red ( $n = 0.060$ ) curve in Fig. 9).

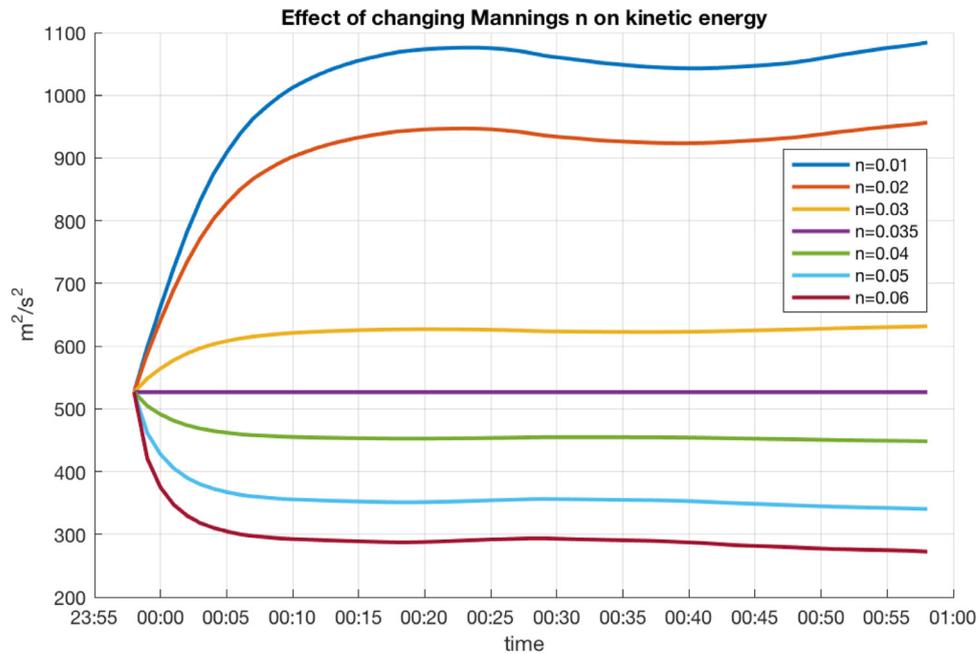
For the first 10 min after the change, the average speed of the drifters released in Edgartown Channel does not depend on the initial value of  $n$  (Fig. 10). The model simulates drifter advection with a 4th order Runge–Kutta scheme with a 1 min time step, and the simulations suggest that changes in the friction in Katama Inlet do not have an effect on the drifters in Edgartown Channel for at least 10 min, consistent with Eq. (4).

It is unsurprising, then, that the assimilation takes longer to converge when the drifter observations are located in the channel than when they are in the inlet: information takes longer to travel between Katama Inlet and Edgartown Channel than it does within the inlet. Due to the nature of the data assimilation method, which combines uncertain forecasts with the noisy observations, the increment made to  $n$  at each analysis step is generally no more than  $0.005 s/m^{1/3}$ . In this regime, there is very little effect on the average drifter speed before fifteen minutes, so the assimilated drifter

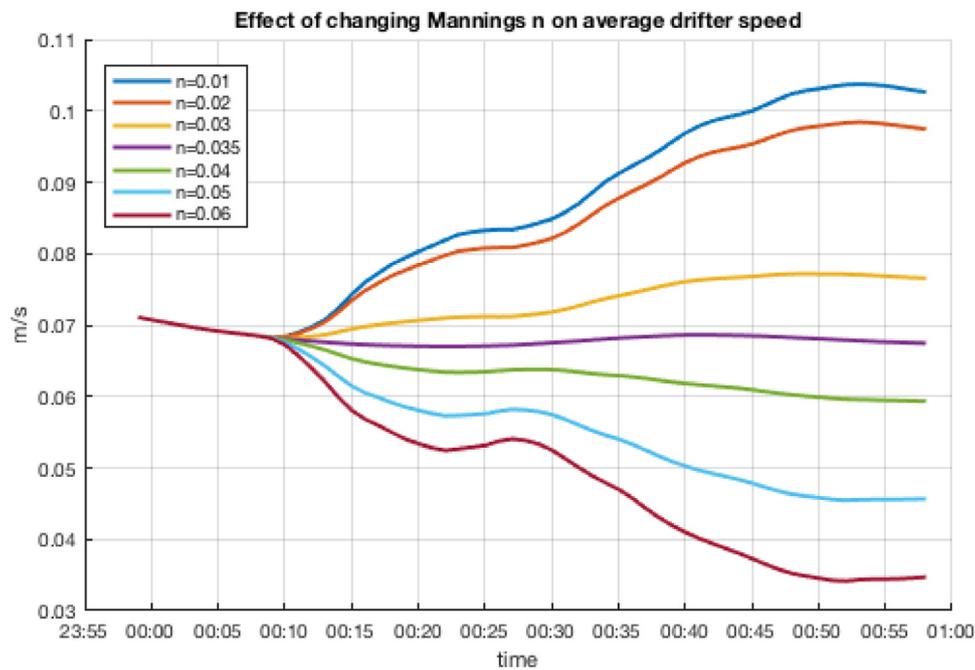
### Kinetic energy, Aug 20 (Edgartown Channel)



**Fig. 8.** Ensemble (thin light red curves) and mean (thick red curves) estimates of kinetic energy versus assimilation time on August 20, when drifters were released in Edgartown Channel, for  $\Delta t=$  (A) 1, (B) 5, and (C) 10 min, as well as the case with no data assimilation (D). The black curves are the synthetic “truth” from the simulation with  $n = 0.035 \text{ s/m}^{1/3}$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 9.** Kinetic energy spatially averaged over the entire domain versus time for different initial values of  $n$  (colors in the legend; units  $s/m^{1/3}$ ) in the inlet. (For interpretation of the references to colour in the text, the reader is referred to the web version of this article.)



**Fig. 10.** Average speed of 13 drifters released in Edgartown Channel versus time for different initial values of  $n$  (colors in the legend) in the inlet. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

trajectories will likely not reflect the changes in  $n$  within one assimilation step of any size studied here. Therefore, small differences in realizations of noise (in the drifter observations) could affect the timescale of convergence of  $n$  fairly strongly when the drifters are in the channel.

To this end, experiments identical to the ones earlier in this section are run (results not shown), but with different realizations of observation noise, sampled from the same Gaussian distribution as the previous experiment. The second experiment with drifters in Katama Inlet performs almost identically to the inlet experiment shown above: the ensemble has converged onto the true value within an hour, with the best performance for  $\Delta t = 1$  min. However, the experiment that assimilates drifters in Edgartown Channel produces fairly different results from the experiment above. For  $\Delta t = 1$  min and  $\Delta t = 5$  min, the ensembles each take about 4 h to converge, more than twice the time for the experiment with  $\Delta t = 1$  min above, but significantly less time than the experiment with  $\Delta t = 5$  min above. The experiment with  $\Delta t = 10$  min results in about a 2.5 h convergence time for the second realization of noise, as compared to the convergence time of 90 min for the original experiment in Section 4.2 (see Fig. 7.) This suggests that the performance of the Edgartown Channel experiments depends strongly on the realizations of observation noise. Ultimately, these results are likely due to subtle interactions between the effects described here; this is typical in data assimilation experiments with nonlinear systems, which often arise in Lagrangian data assimilation.

## 5. Results from a field experiment

### 5.1. Setup

The trajectories of surface drifters released in Katama Inlet on August 22 (Inlet Trajectories in Fig. 3) and in Edgartown Channel August 20 (Channel Trajectories in Fig. 3) are assimilated to estimate the friction in Katama Inlet. Prior to reviewing the results of the assimilation, the performance of the model is tested with the original value  $n = 0.035$  s/m<sup>1/3</sup>. The simulated kinetic energy from

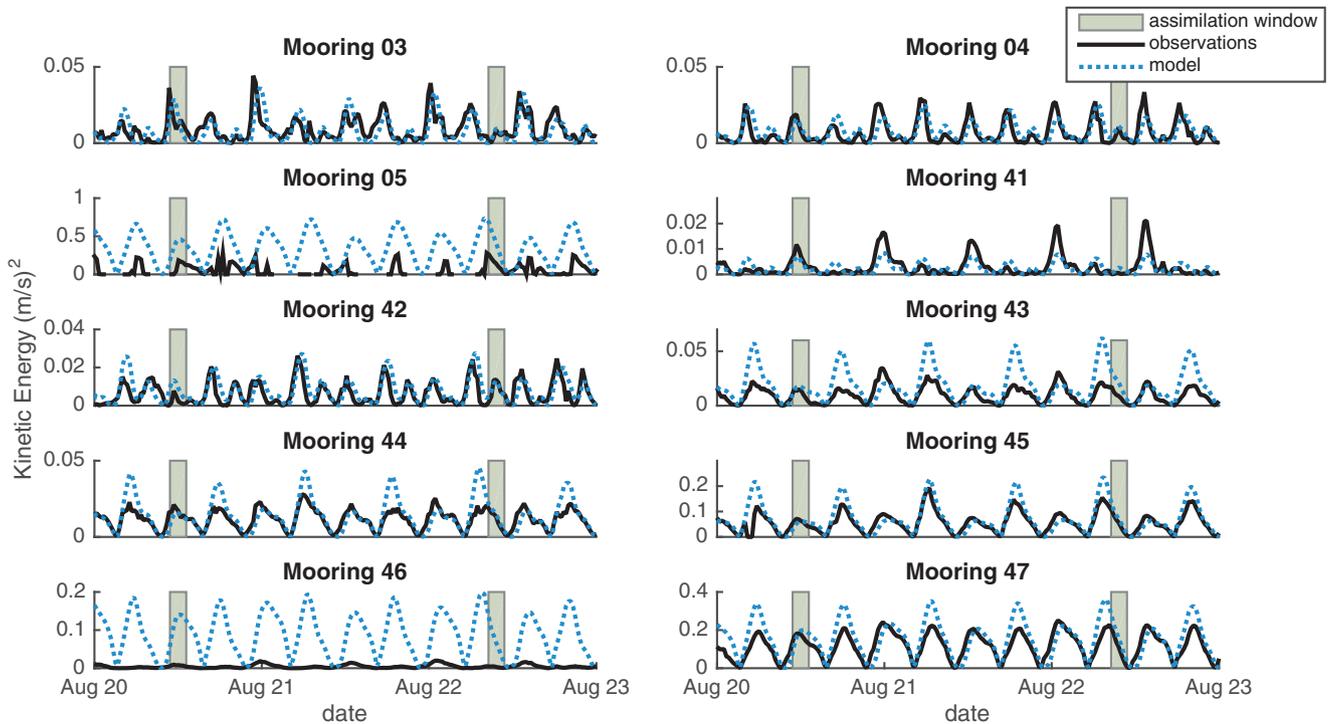
that experiment in the inlet is compared with the kinetic energy observed at 10 locations in the system (Fig. 11). The model kinetic energy at each sensor location is calculated by interpolating the simulated velocity between nearby grid points. The observed kinetic energy is calculated from currents measured about 0.8 m above the seafloor in water depths < 2 m and from a depth average of the nearly uniform-in-the-vertical profiles in depths > 2 m (Orescanin et al., 2014).

The largest discrepancies between simulations with  $n = 0.035$  and observations are at locations 05 and 46, both close to Katama Inlet (Fig. 3). The value  $n = 0.035$  s/m<sup>1/3</sup> was based on observations in 2011, but the inlet lengthened, narrowed, and shoaled by 2013, resulting in a significant change in  $n$  (Orescanin et al., 2016). Instead of re-tuning  $n$  with the 2013 in-situ observations,  $n$  is estimated by assimilating drifter trajectories into the model.

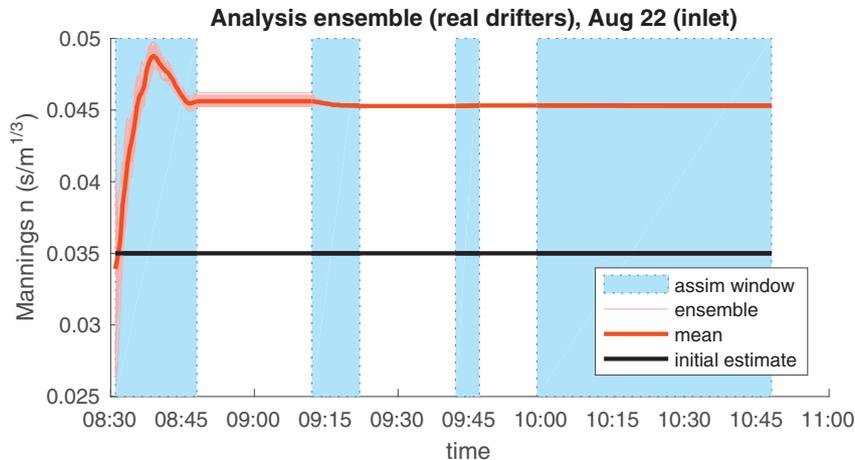
Two experiments are performed – the first assimilates drifter observations in Katama Inlet, and the second assimilates drifter observations in Edgartown Channel. The model ensemble is initialized with a mean of  $n = 0.035$  s/m<sup>1/3</sup> and a standard deviation of 0.005 s/m<sup>1/3</sup>. The observation error is set at  $\sigma_R = 25$ m, as in the synthetic experiments.

Drifter data are available every second, but results from the synthetic runs (Section 4) suggest that this is more frequent than necessary since assimilating data every 1 min was sufficient for successful estimation in those experiments. Additionally, the EnKF assumes that observation errors are uncorrelated in time; if drifter positions are sampled every 1 sec, it is not clear that this assumption will hold. Thus,  $\Delta t = 1.0$  min for the channel drifter data on August 20, and  $\Delta t = 0.5$  min for the inlet drifter data on August 22 due to the shorter trajectories (Fig. 3). Synthetic experiments with  $\Delta t = 0.5$  min for the inlet drifters (not shown) demonstrate very similar results to those with  $\Delta t = 1.0$  min.

On August 20, ten drifters were deployed in the channel at 10:50 am and recovered at 1:10 pm. On August 22, the drifters were deployed in several relatively short releases in the inlet. Twelve drifters are assimilated from 8:31 until 8:48 am (Assimilation Round 1), at which point each ensemble member is evolved forward until 9:12 am with the final estimate of friction from



**Fig. 11.** Observed (solid black curves) and simulated (dashed blue curves,  $n = 0.035$ ) kinetic energy versus time for 3 days in 2013. The shaded boxes are times during which drifters were deployed. The location of each comparison is given by the mooring number at the top of each panel, which corresponds to a sensor on the map in Fig. 3. Note differences in scales of y-axes. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 12.** Ensemble (thin light red curves) and mean (thick red curves) estimates of Manning's  $n$  from assimilating drifters within Katama Inlet versus time, with the initial estimate of  $n = 0.035 \text{ s/m}^{1/3}$  (black horizontal line, the value found for the 2011 data (Orescanin et al., 2016)). Blue shaded regions are assimilation windows and unshaded regions are time periods in which the ensemble estimates of  $n$  were kept constant. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Round 1. At 9:12 am, the next wave of ten drifters are assimilated for 10 min (Round 2). In Round 3, nine drifters are assimilated from 9:42 until 9:47am, and in Round 4, nine drifters are assimilated from 9:59 until 10:20 am. Note that the number of drifters assimilated in each round is not constant, because not every drifter was released at the exact same time nor did they all provide meaningful trajectories. Thus, only drifters that provided trajectories during overlapping time windows are assimilated.

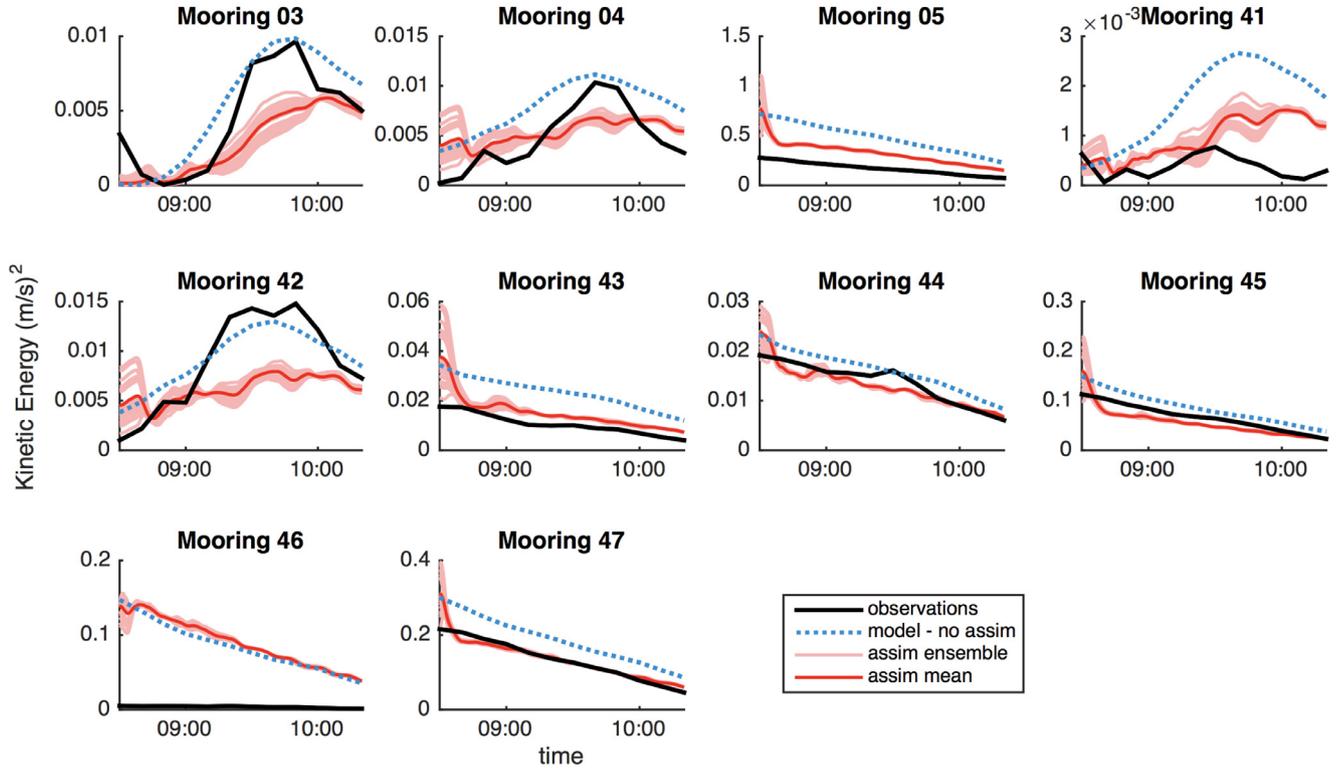
## 5.2. Results and discussion

Manning's  $n$  estimated by assimilating the Inlet Trajectories converges to  $n = 0.045 \text{ s/m}^{1/3}$  (Fig. 12), higher than the 2011 es-

timated value of  $0.035 \text{ s/m}^{1/3}$  (Orescanin et al., 2016). Without assimilation and with  $n = 0.035$ , the model over-predicts the kinetic energy at almost every in-situ sensor location (Fig. 13). By assimilating drifter data, the model is closer to the in-situ observations at most locations, especially at sensors 05 and 47, located close to Katama Inlet (Fig. 3). Specifically, since the observed drifters are traveling more slowly than the simulated drifters within the assimilation, the EnKF analysis increases the drag coefficient to diminish the mismatch between the observed drifters and the simulated drifters.

Figs. 12 and 13 show how the estimate of  $n$  and the associated kinetic energy change during assimilation, as  $n$  is updated. In addition, another simulation is restarted on August 20

## Aug 22 (inlet drifters)



**Fig. 13.** Kinetic energy versus time for observations (black curves), the model with no assimilation and  $n = 0.035 \text{ s/m}^{1/3}$  (dashed blue curves), and ensemble (thin light red curves) and mean (thick red curve) estimates of  $n$  from assimilating drifters within Katama Inlet on August 22 versus time at each sensor location (numbers on top of each panel refer to sensor locations in the map in Fig. 3). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

and run for three full days with the final estimated value of  $n = 0.045 \text{ s/m}^{1/3}$ . Model skill is quantified by the root mean square error (RMSE, averaged over August 20–22) in kinetic energy relative to that observed with the in-situ sensors. At each sensor location, the observed kinetic energy at time  $t$  is calculated as  $KE_{obs}(t) = 1/2(u_{obs}(t)^2 + v_{obs}(t)^2)$  for  $u_{obs}, v_{obs}$  observed latitudinal and meridional current velocities, respectively. Similarly, the modeled kinetic energy  $KE_{sim}(t) = 1/2(u_{sim}(t)^2 + v_{sim}(t)^2)$  is calculated by interpolating the simulated velocity to the sensor locations. The RMSE is defined as

$$RMSE = \left( \frac{\sum_{t=t_0}^{t_f} (KE_{obs}(t) - KE_{sim}(t))^2}{\sum_{t=t_0}^{t_f} (KE_{obs}(t))^2} \right)^{1/2} \quad (5)$$

over the time period from  $t_0$  to  $t_f$ . Relative to the simulation with  $n = 0.035 \text{ s/m}^{1/3}$ , the simulation with the assimilated parameter  $n = 0.045 \text{ s/m}^{1/3}$  yields improved kinetic energy estimates at nearly every mooring, with the most significant improvement at Mooring 05, in Katama Inlet (Table 1).

In contrast, the estimate of  $n$  in Katama Inlet from assimilating drifter trajectories in Edgartown Channel does not converge, and at the end of the time window  $n = 0.018 \text{ s/m}^{1/3}$  (Fig. 14), significantly lower than the value estimated by assimilating drifters in the inlet, and lower than the initial estimate of  $n = 0.035 \text{ s/m}^{1/3}$ . Unlike at the time of the Katama Inlet drifters' release, at the time of the drifters' release in Edgartown Channel the model simulation underestimates the observed kinetic energy at 7 of the 10 in-situ sensors (Fig. 15). In particular, the original model underestimates the kinetic energy at sensors 03, 04, and 41 in Edgartown Channel (see Fig. 3 for locations), where the drifters were released, although the kinetic energy at sensor 42 (also near the channel) is

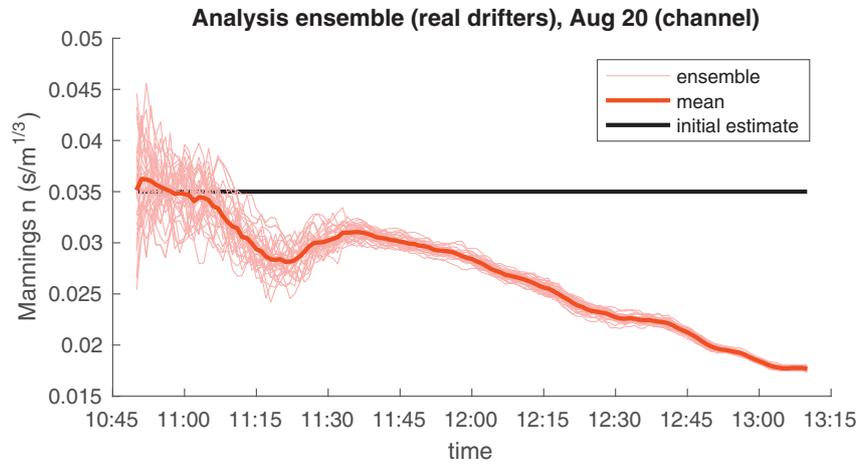
**Table 1**

Normalized root mean squared error of kinetic energy between model simulations with given  $n$  (units  $\text{s/m}^{1/3}$ ) and the in-situ observations between August 20 and 22.

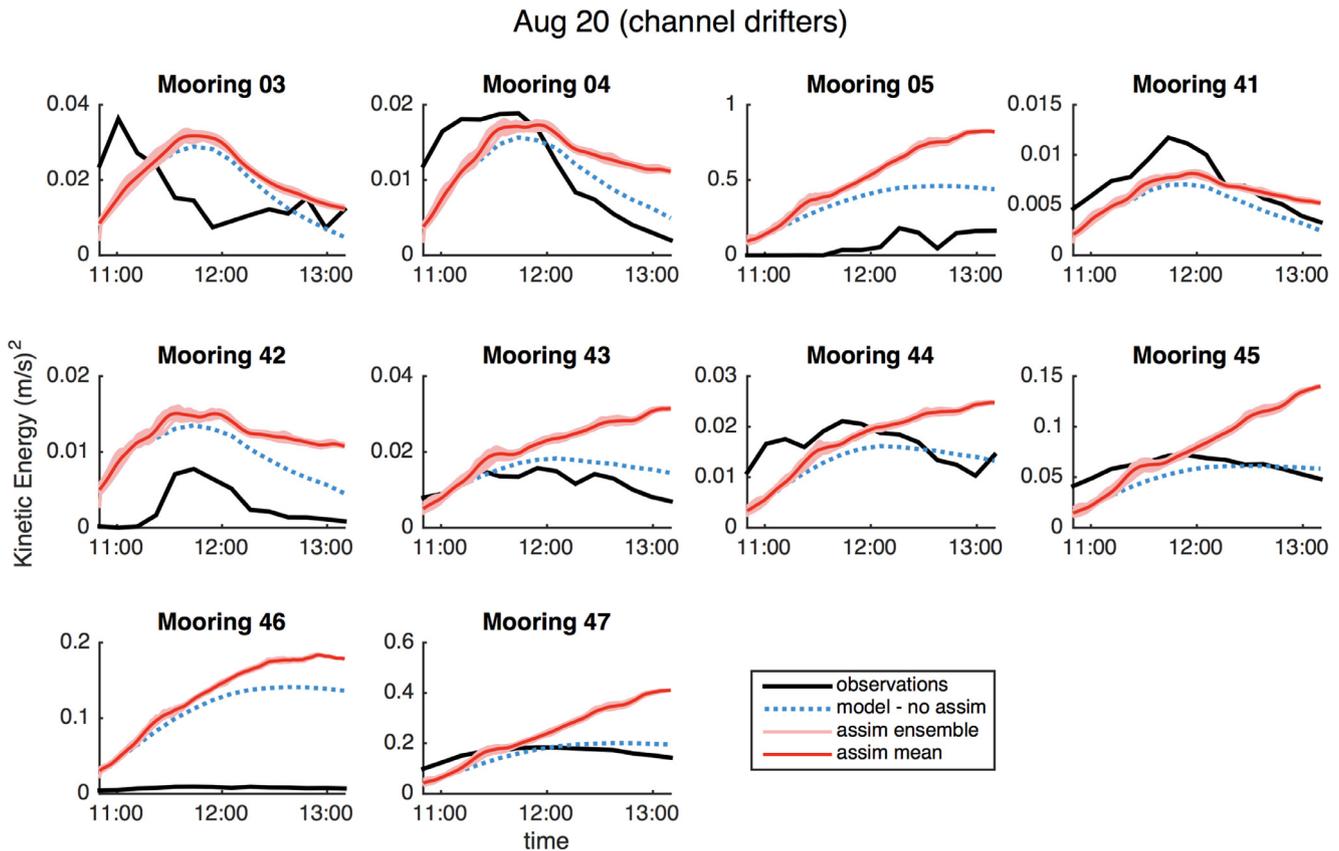
Sensor	$n = 0.035$	$n = 0.018$	$n = 0.045$
03	0.007	0.013	0.007
04	0.006	0.012	0.005
05	0.371	0.888	0.234
41	0.003	0.003	0.004
42	0.005	0.013	0.004
43	0.014	0.042	0.007
44	0.007	0.014	0.006
45	0.035	0.105	0.025
46	0.100	0.096	0.095
47	0.067	0.179	0.045

overestimated. The assimilation seeks to diminish this initial mismatch between the observed and simulated drifter trajectories by increasing the kinetic energy via decreasing the drag coefficient. As a result, towards the end of the assimilation period, both the original simulation with  $n = 0.035 \text{ s/m}^{1/3}$  and the assimilated simulations overestimate the observed kinetic energy (Fig. 15).

The model run with the final value of  $n = 0.018 \text{ s/m}^{1/3}$  has higher RMSE relative to the observed kinetic energy than the model using  $n$  estimated by assimilating drifters in the inlet (Table 1), with the biggest errors at sensor 05 in the inlet. To test if the initial discrepancy in kinetic energy is indeed a driving factor in the results of the assimilation, channel drifters are assimilated beginning at 12:00 pm (rather than at 10:50 am), when the model changes from underestimating the observed kinetic energy to either overestimating or accurately estimating the observed energy



**Fig. 14.** Ensemble (thin light red curves) and mean (thick red curve) estimates of Manning's  $n$  in Katama Inlet from assimilating drifters in Edgartown Channel on August 20 as a function of time. The black line is the initial estimate  $n = 0.035 \text{ s/m}^{1/3}$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

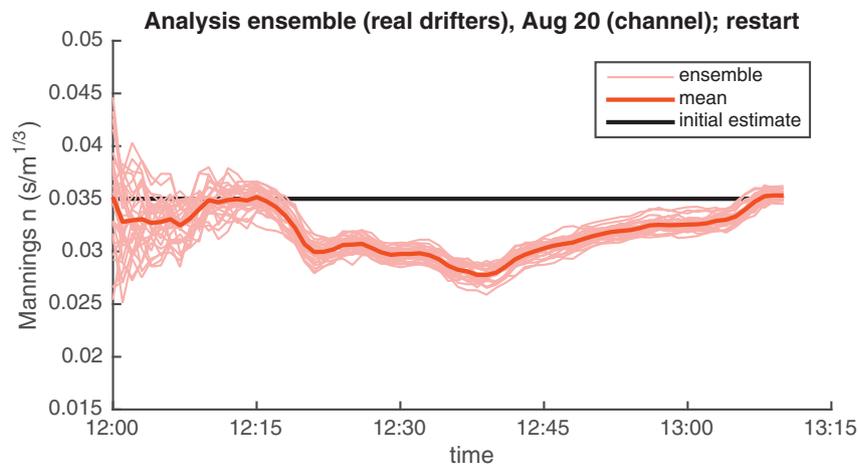


**Fig. 15.** Kinetic energy versus time for observations (black curves), the model with no assimilation and  $n = 0.035 \text{ s/m}^{1/3}$  (dashed blue curves), and ensemble (thin light red curves) and mean (thick red curve) estimates of  $n$  in the inlet from assimilating drifters within Edgartown Channel on August 20 versus time at each sensor location (numbers on top of each panel refer to sensor locations in the map in Fig. 3). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

(Fig. 15). The model is initialized with  $n = 0.035 \text{ s/m}^{1/3}$ , and run over the window from 12:00 to 1:10 pm (Fig. 16).

In this case, the estimate of  $n$  oscillates and decreases initially, and after 1 hr returns to the initial value of  $n = 0.035 \text{ s/m}^{1/3}$  (although the ensemble may not have converged; Fig. 16). This is because the model is not consistently over- or under-estimating the observed kinetic energy at the start of the window, and thus the assimilated ensemble does not increase or decrease the estimate of  $n$  by the end of the assimilation.

These results suggest that the assimilation outcome can depend on the time and location of drifter deployment. Because the parameter of interest is the friction in a specific part of the domain (Katama Inlet), when drifters are deployed near or in that region, the assimilation performs better. For the experiments with drifters deployed in Edgartown Channel, the results depend on when the assimilation begins. This is linked to whether the model over- or under-estimates the kinetic energy at the beginning of the assimilation window. Further experiments would help determine the rel-



**Fig. 16.** Ensemble (thin light red curves) and mean (thick red curve) estimates of Manning's  $n$  in Katama Inlet from assimilating drifters in Edgartown Channel beginning at 12:00 pm on August 20 versus time. The black line is the initial estimate  $n = 0.035 \text{ s/m}^{1/3}$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

ative importance of drifter deployment location and the difference in observed and simulated kinetic energy at the beginning of the assimilation window.

Note that these experiments do not include any covariance localization, a common method for reducing artificial correlations between spatially-distant regions of the domain, since the parameter of interest covers an entire subregion that may or may not include the drifter trajectories. Thus, these results demonstrate how the assimilation behaves when drifter observations in Edgartown Channel are allowed to update  $n$  in Katama Inlet without any constraints. Imposing localization in the Edgartown Channel experiments would likely slow the time to convergence without changing the overall behavior of the ensemble estimate of  $n$ .

## 6. Conclusions

Trajectories of drifters are assimilated into a numerical model (ADCIRC) to estimate the friction (Manning's  $n$ ) in Katama Inlet, which affects circulation in tidally-dominated Katama Bay. Synthetic observation experiments demonstrate the ability of the assimilation method to estimate Manning's  $n$  using only trajectories of passive Lagrangian drifters. The performance of the assimilation is greatest when the drifters are located near the region for which  $n$  is estimated. When the synthetic drifters are located in a different region (Edgartown Channel), away from the Katama Inlet region for which  $n$  is estimated, the assimilation performance decreases, likely owing to interactions between the intrinsic adjustment time of the bay, sensitivity to observational noise, and nonlinear effects within the data assimilation method. This is supported by the investigations with identical setups but different realizations of observational noise (Section 4.3): the two realizations of the Katama Inlet experiment were qualitatively indistinguishable, while the two Edgartown Channel experiments differed significantly.

There are larger differences in the outcomes when real drifter data are assimilated, depending on whether drifters from Katama Inlet or Edgartown Channel are assimilated. Assimilation of trajectories observed from drifters released near Katama Inlet converges to a larger inlet drag coefficient than the 2011 value. Throughout the system, the corresponding simulated kinetic energy with the assimilated  $n$  is often closer to the observed kinetic energy than simulations with the 2011 value. In contrast, when trajectories observed from drifters released in Edgartown Channel in 2013 are assimilated,  $n$  is reduced and the kinetic energy estimates are not as

accurate. This is partially due to the mismatch between the simulated (initialized with the 2011 value of  $n$ ) and observed kinetic energy at the beginning of the assimilation window, and partially due to the larger spatial distance between the observations and the region for which  $n$  is estimated. These results are also sensitive to the time the drifters are released in the channel.

Differences in assimilation performance between the synthetic and real experiments are likely due to unmodeled processes in the real experiment that may have a larger effect on the assimilation when the observations are far from the region of interest, owing to higher sensitivity to noise. Thus, an OSSE's ability to provide guidance decreases with increasing distance between observations and the region of interest.

The initial numerical circulation model used bathymetry measured in 2013 and a parameter tuned for kinetic energy measurements in 2011. The Katama Bay domain changed significantly in the area of Katama Inlet between 2011 and 2013 (recall Fig. 1B and C), and the goal was to improve the parameter estimate  $n$  from 2011 to represent the 2013 situation. Results depend on both when and where drifters are observed: if one wishes to estimate a local parameter in a model, then it is best to deploy drifters in that region. Ultimately, assimilation of real drifter trajectory data in Katama Inlet provides an improved estimate of  $n$  in the inlet, based on comparisons between observed kinetic energy in 2013 and kinetic energy from the model simulations with the 2011 and 2013 estimates of the parameter. While Eulerian data are used to judge the performance of the assimilation, they are not necessary for the actual computation of the parameter.

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